

Larger transfers financed with more progressive taxes? On the optimal design of taxes and transfers

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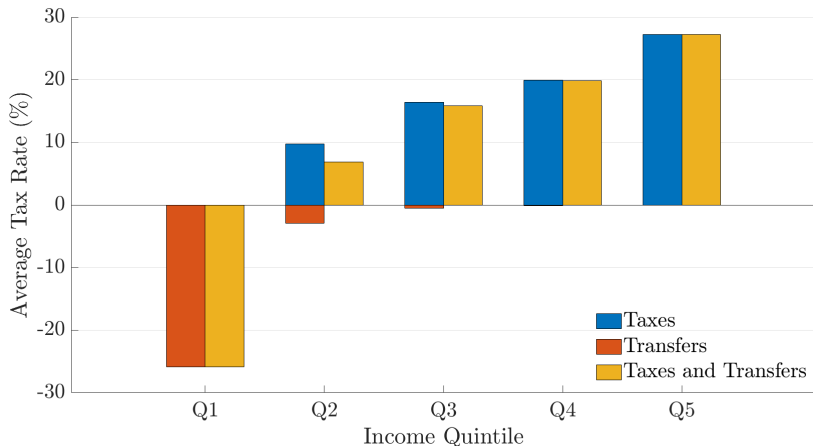
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November 2021

These views are those of the authors and not necessarily those of the Board of Governors or the Federal Reserve System.

Redistribution in the U.S.

- **Taxes** and **transfers** are two key components in the U.S. fiscal system



- Working-age households ranked by income quintiles (CBO, 2013)

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 - **Analytical**: How should **tax progressivity** change with **more generous transfers**?

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 - Rich quantitative macro model
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- Two questions
 - Analytical: How should tax progressivity change with more generous transfers?
 - Quantitative: How generous should transfers be? How progressive should taxes be?

Theoretical analysis

- Simple model with progressive income tax scheme & a transfer
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 - Optimal negative relationship between T and τ
 - Due to both redistribution and efficiency concerns
- ⇒ **Optimal** fiscal plan features large average but low marginal progressivity

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 - Rich earnings dynamics: Pareto tail and GMAR process
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- ⇒ Large **welfare gains**!

■ Evolution of inequality and taxation in the US

Piketty and Saez (2003), Piketty and Saez (2007), Piketty, Saez, and Zucman (2017), Splinter (2020)

■ Parametric tax functions: Empirical estimates

Gouveia and Strauss (1994), Guner, Kaygusuz, and Ventura (2014), Feenberg, Ferriere, and Navarro (2020)

■ Analytical frameworks to evaluate optimal tax progressivity

Heathcote, Storesletten, and Violante (2014, 2017)

■ Quantitative frameworks to evaluate optimal tax progressivity

Bakış, Kaymak, and Poschke (2015), Guner, Lopez-Daneri, and Ventura (2016), Krueger and Ludwig (2016), Peterman (2016), Kindermann and Krueger (2021), Boar and Midrigan (2021), Guner, Kaygusuz and Ventura (2021)

■ Intersection of Ramsey (1927) and Mirrlees (1971) traditions

Findeisen and Sachs (2017), Heathcote and Tsujiyama (2021)

An Analytical Model

A tractable environment

Static Bewley-Hugett economy

- No capital, representative **firm** with linear production in labor

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 - Raises loglinear taxes: $\mathcal{T}(y) = y - \lambda y^{1-\tau}$
 - Budget: $G + T = \int y_{it} di - \lambda \int y_{it}^{1-\tau} di$

► Graph

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- A continuum of infinitely-lived **workers**

- **Wages** AR(1): $\log z_{it} = \rho_z \log z_{it-1} + \omega_{it}$, with $\omega_{it} \sim \mathcal{N}\left(-\frac{v_\omega}{2(1+\rho_z)}, v_\omega\right)$

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⇒ **Next**: 1) RA case $v_\omega = 0$, 2) HA with $T = 0$, and 3) HA with $T \neq 0$

Transfers

Welfare: Representative agent

- Representative agent $v_\omega = 0$
- Optimal fiscal plan attains the first-best allocation $n^*(G)$

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\Rightarrow **Negative** relationship between τ and T due to **efficiency** concerns

- **Efficiency** gains of T are **decreasing** in τ

No transfers

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$$\mathcal{W}(\tau) = \underbrace{\log(n_0(\tau) - G)}_{\text{Size}} \underbrace{- \frac{1-\tau}{1+\varphi}}_{\text{Labor disutility}} \underbrace{- (1-\tau)^2 \frac{v_\omega}{2(1-\rho_z^2)}}_{\text{Redistribution}}$$

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Efficiency

- Two **efficiency** terms
 - **Size** term \downarrow with τ ; **Labor disutility** term \uparrow with τ

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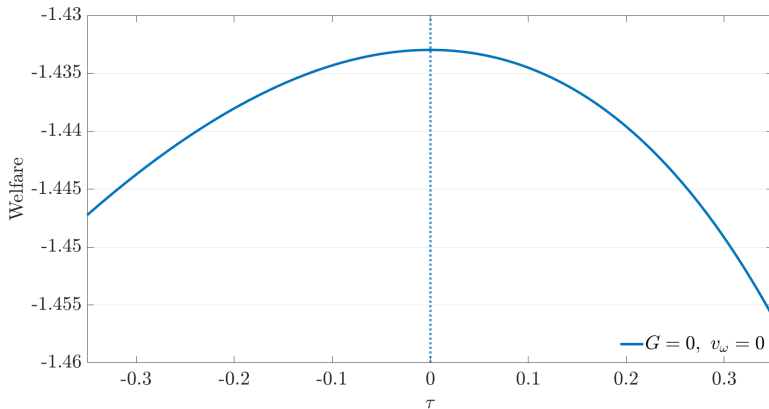
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Welfare without transfers

Optimal τ

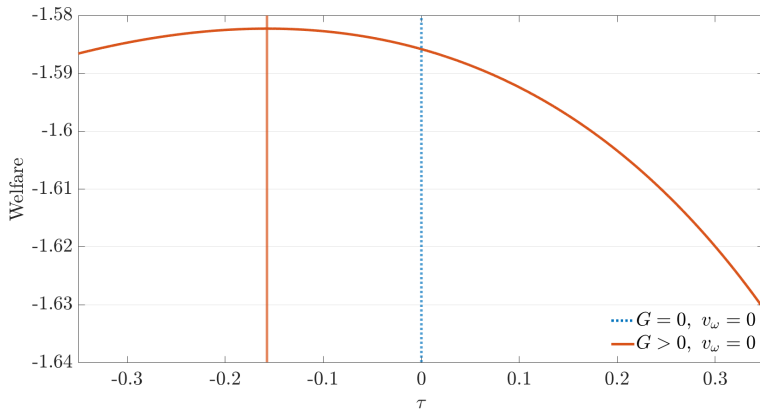
- No spending, no heterogeneity: $\tau = 0$

► Calibration



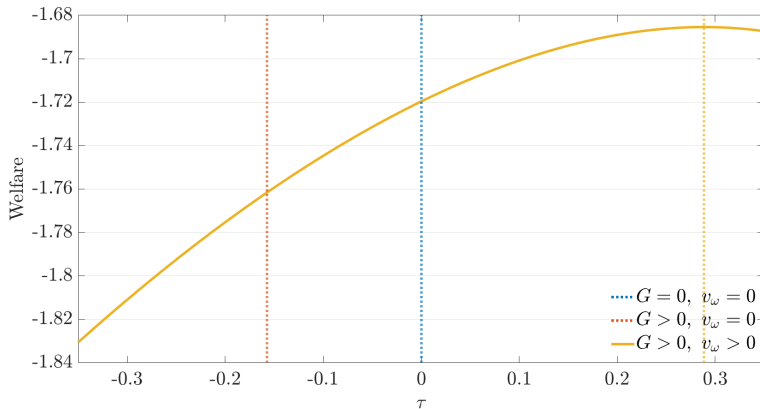
Welfare without transfers Optimal τ

- Positive spending, no heterogeneity: $\tau < 0$



Welfare without transfers Optimal τ

- Spending, **uninsurable shocks**: $\tau > 0$



- **Implicit function theorem:** approximation of the FOC

$$\hat{n}_{it} \approx n_0(\tau) - \frac{T}{1 + \varphi} \frac{n_0(\tau)}{n_0(\tau) - G} \exp \left(-\tau(1 - \tau) \frac{v_\omega}{1 - \rho_z^2} \right) z_{it}^{-(1-\tau)}$$

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- Approximated formula with heterogeneity $v_\omega > 0$

$$W(\tau, T) = W(\tau, 0) + T \left[\Omega^e(\tau, v_\omega) + \Omega^r(\tau, v_\omega) \right],$$

where the two terms capture

- **Efficiency** concerns
- **Redistribution** concerns ($\Omega^r(\tau, v_\omega) = 0$ when $v_\omega = 0$)

Transfers

Welfare: Efficiency

- Efficiency: $\Omega^e(\tau, v_\omega) = \Omega_e^{ra}(\tau) + \Omega_e^{ha}(\tau, v_\omega)$
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$$\begin{aligned}\Omega_e^{ra}(\tau) &\equiv \underbrace{-\frac{n_0(\tau)}{n_0(\tau) - G} \frac{1}{1 + \varphi} \frac{1}{n_0(\tau) - G}}_{\text{Size} < 0} + \underbrace{\frac{1 - \tau}{1 + \varphi} \frac{1}{n_0(\tau) - G}}_{\text{Labor disutility} > 0} \\ &= U_c(C_0(\tau)) \left. \frac{\partial Y^{ra}(\tau, T)}{\partial T} \right|_{T=0} + U_n(n_0(\tau)) \left. \frac{\partial n^{ra}(\tau, T)}{\partial T} \right|_{T=0}\end{aligned}$$

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- $\Omega_e^{ra} = 0$ when $\tau = \tau_0^*(G)$, and decreases with τ (first-best)
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- Additional **efficiency** Ω_e^{ha} term with heterogeneous agents ... **numerically small**

Transfers

Welfare: Redistribution

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$$\begin{aligned}\Omega_r(\tau, v_\omega) &= \frac{(1 - \tau)^2}{n_0(\tau) - G} \frac{v_\omega}{1 - \rho_z^2} \\ &= \mathbb{E}[U_c(c_0(\tau))] - U_c(C_0(\tau))\end{aligned}$$

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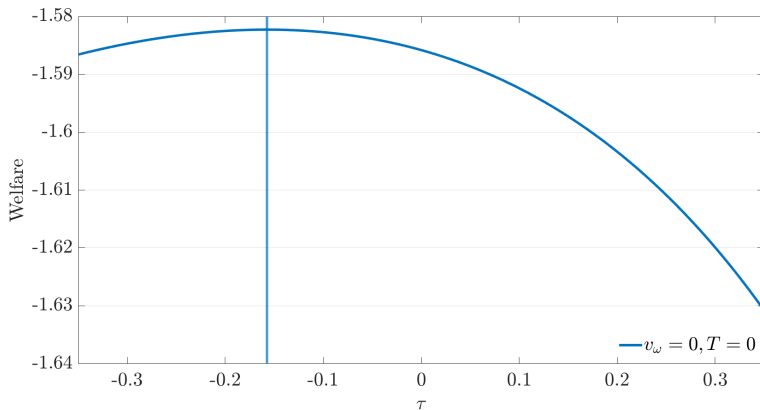
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\Rightarrow **Redistribution** gains of T are **decreasing** in τ

\Rightarrow **Negative** optimal relationship between T and τ

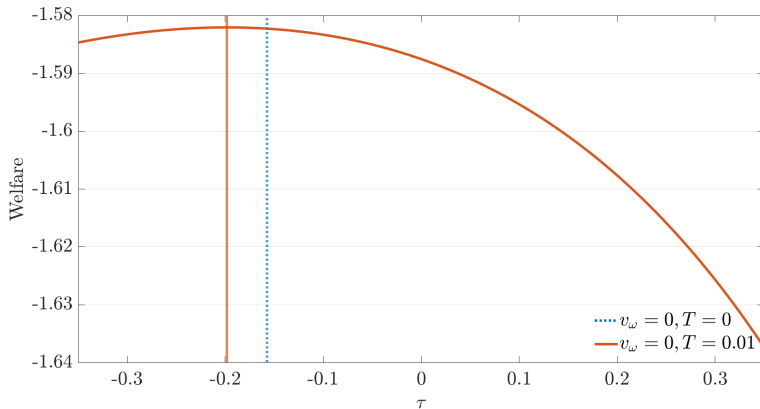
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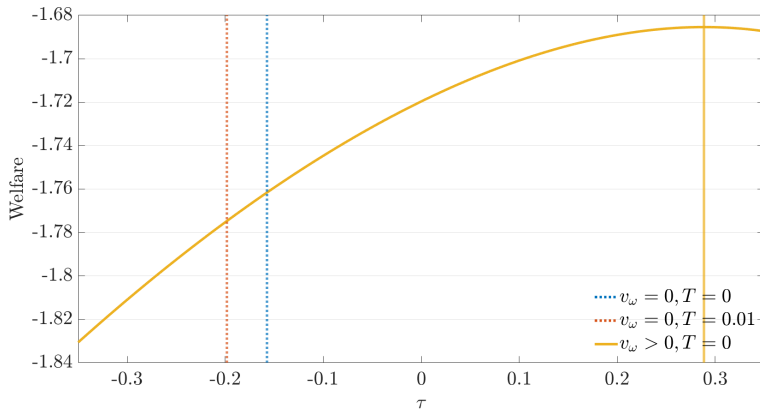
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- Spending, no heterogeneity, $T > 0 \Rightarrow$ lower τ



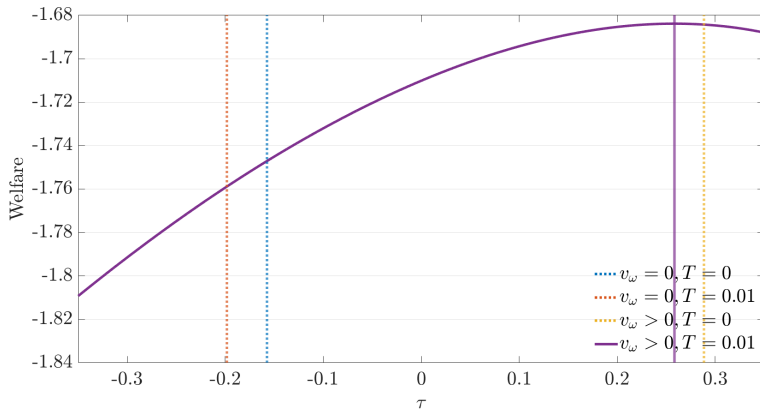
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■ Spending, idiosyncratic shocks



Transfers Heterogeneous agents

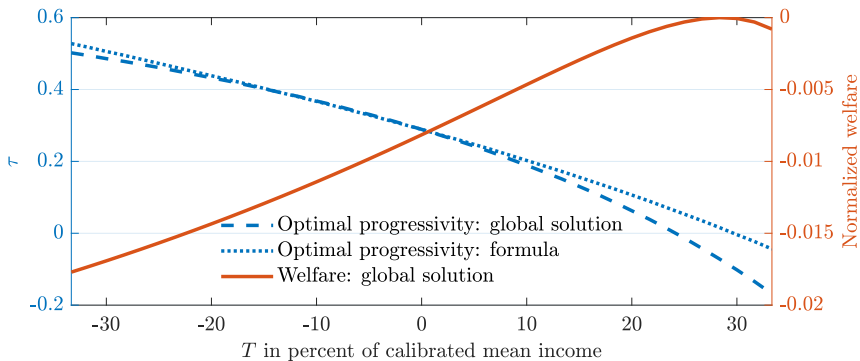
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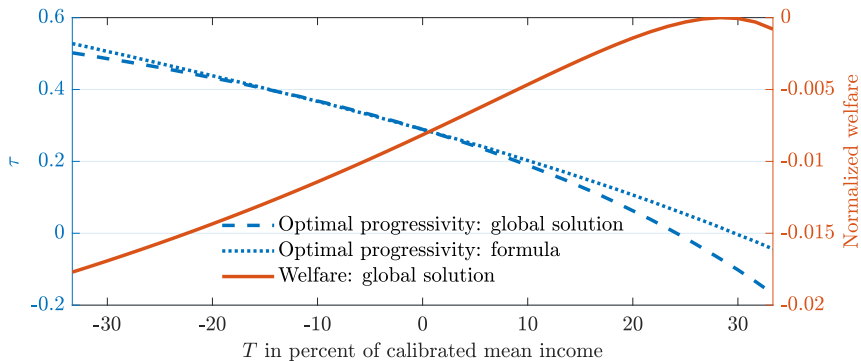
- A **negative** relationship between τ and T



Transfers

Heterogeneous agents

- A **negative** relationship between τ and T



- Formula: a good **approximation**!

Optimal plan with transfers

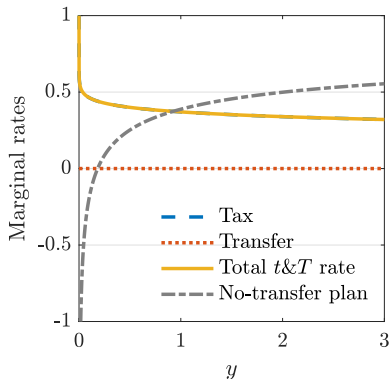
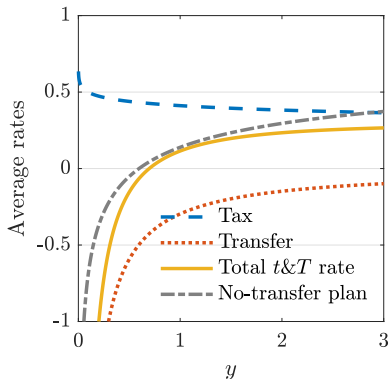
Global solution of the static model

- Generous transfers: $T = 0.3$, regressive income taxes: $\tau = -0.08$

Optimal plan with transfers

Global solution of the static model

- Generous transfers: $T = 0.3$, regressive income taxes: $\tau = -0.08$



- Average taxes are increasing, marginal taxes are decreasing

Taking stock

- Optimal **negative relationship** between **progressivity** and **transfers**
 - Due to both efficiency and redistribution
- The optimal plan looks **very different** when allowing for transfers
 - Break the link between average and marginal t & T rates

A Quantitative Model

Overview

- Rich quantitative model
 - **Benchmark** economy: standard Aiyagari with
 - + Realistic income risk: Gaussian mixture autoregressive (GMAR)
 - + Income concentration: Pareto tail
 - Extension: heterogeneous discount factors
- Calibration to the U.S.
- **Optimize** on the **fiscal system** parameters
 - Global algorithm: TikTak
 - Taking into account **transitions**

Households, firm, government

- Household's value function with productivity z and assets a :

$$V(a, z) = \max_{c, a', n} \left\{ \frac{c^{1-\sigma}}{1-\sigma} - B \frac{n^{1+\varphi}}{1+\varphi} + \beta \mathbb{E}_{z'} [V(a', z') | z] \right\}$$

s.t.

$$c + a' \leq wz n + (1+r)a - \mathcal{T}(wzn, ra), \quad a' \geq 0$$

- Productivity z follows a stochastic process

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- **Government's** budget constraint:

$$G + (1+r)D = D + \int \mathcal{T}(wzn, ra) d\mu(a, z)$$

Fiscal system Taxes

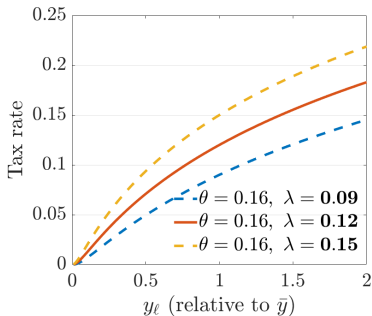
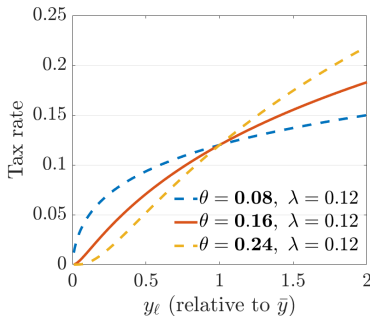
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Fiscal system Taxes

- Flat **capital** tax: $\tau_k y_k$, with $\tau_k = 35\%$
- Progressive **labor** tax: $\exp\left(\log(\lambda) \left(\frac{y_\ell}{\bar{y}}\right)^{-2\theta}\right) y_\ell$
 - λ is the tax rate at $y_\ell = \bar{y}$, θ captures the **progressivity**

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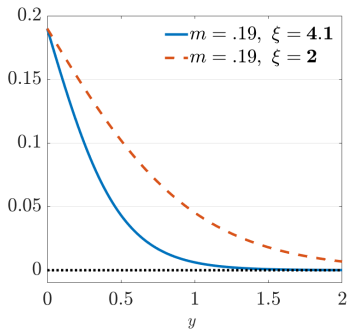
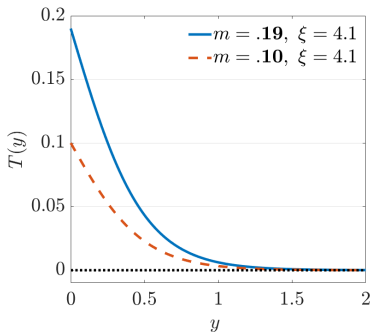
- Interpretation: θ and τ on a roughly similar scale

► Graph

Fiscal system Transfers

■ New targeted-transfers function: $m\bar{y} \frac{2 \exp\left\{-\xi\left(\frac{y}{\bar{y}}\right)\right\}}{1 + \exp\left\{-\xi\left(\frac{y}{\bar{y}}\right)\right\}}$

- m is the level at $y = 0$, ξ is the speed of phasing-out



- Log-productivity follows a **Gaussian Mixture Autoregressive Process**

$$\log z_t = \rho \log z_{t-1} + \eta_t,$$

$$\eta_t \sim \begin{cases} \mathcal{N}(\mu_1, \sigma_1^2) & \text{with probability } p_1, \\ \mathcal{N}(\mu_2, \sigma_2^2) & \text{with probability } 1 - p_1 \end{cases}$$

Güvenen, Karahan, Ozkan, and Song (2021)

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- 5 parameters: $(\rho, p_1, \mu_1, \sigma_1, \sigma_2)$

- Restriction: $\mu_2 = -\frac{p_1}{1-p_1}\mu_1 \Leftarrow \mathbb{E}(\eta_t) = 0$

Calibration

- Income process to match household income risk
 - Annual earnings growth distribution from PSID (1978-1992)
 - + Std deviation: 0.35, Skewness: -0.45, Kurtosis: 12, P9010: 0.64
 - And top-10 labor income share: 38%

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- **Preferences**: $\sigma = 2$, $\varphi^{-1} = 0.4$; β to match $r = 2\%$

► More

Income and Wealth Distributions

Data	Q1	Q2	Q3	Q4	Q5	Top 10
Labor income	4%	9%	14%	21%	52%	38%
Net worth	-1%	1%	3%	9%	88%	71%
Baseline	Q1	Q2	Q3	Q4	Q5	Top 10
Labor income	4%	9%	14%	20%	52%	38%
Net worth	0%	2%	8%	18%	72%	52%

Notes: Labor income shares by labor-income quintiles and wealth shares by wealth quintile, households aged 25-60. Data: SCF 2013.

- Labor elasticity at the top-1%: 0.20

Average Tax and Transfer Rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	0%	10%	16%	20%	27%
Transfer rate	26%	3%	1%	0%	0%
Model	Q1	Q2	Q3	Q4	Q5
Tax rate	8%	11%	14%	17%	28%
Transfer rate	24%	4%	1%	0%	0%

Notes: Average tax rates paid and transfer rates received per income quintile.

Data: CBO 2013, working-age households. Model: tax parameters: $\theta = 0.16$, $\lambda = 0.12$; transfer parameters: $m = 0.19$, $\xi = 4.1$.

► Graph

Optimal tax-and-transfer plan

- The **optimal plan** features

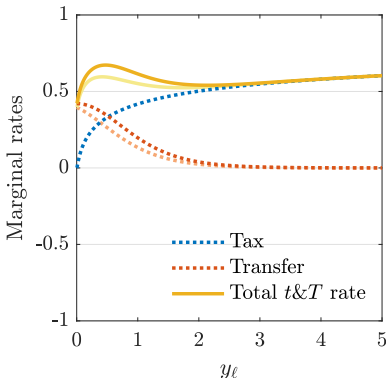
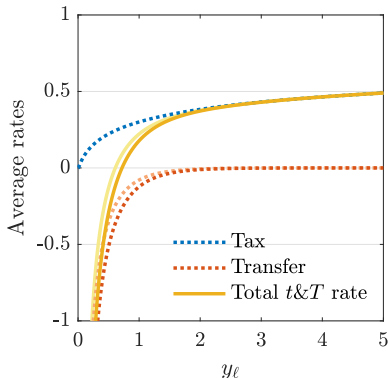
Optimal tax-and-transfer plan

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Optimal tax-and-transfer plan

■ The optimal plan features

- Large transfers $m = 0.46$, with a slow phase-out $\xi = 1.94$
- Moderate tax progressivity, close to the calibrated value $\theta = 0.17$



- Graph for $y_k = 0$ and y_ℓ normalized by \bar{y}

Optimal plan Average and marginal rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	0%	10%	16%	20%	27%
Transfer rate	26%	3%	1%	0%	0%

Optimal	Q1	Q2	Q3	Q4	Q5
Tax rate	15%	21%	27%	31%	44%
Transfer rate	170%	58%	21%	6%	0%

-
-
- Transfer \$26*k* for lowest income hh, and \$7.4*k* for median.
 - Much **larger redistribution** overall ...

Optimal plan Average and marginal rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	0%	10%	16%	20%	27%
Transfer rate	26%	3%	1%	0%	0%
Total avg rate	-26%	-7%	15%	20%	27%
Optimal	Q1	Q2	Q3	Q4	Q5
Tax rate	15%	21%	27%	31%	44%
Transfer rate	170%	58%	21%	6%	0%
Total avg rate	-155%	-37%	6%	25%	44%

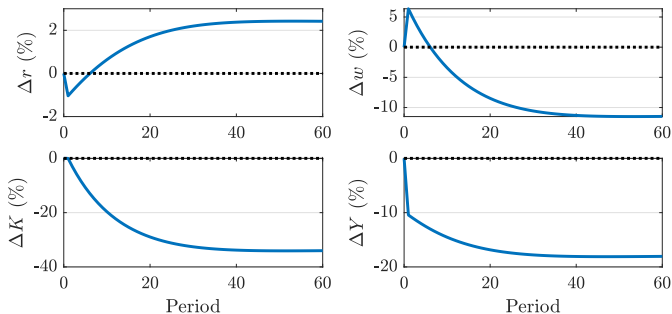
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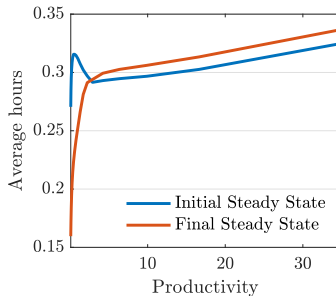
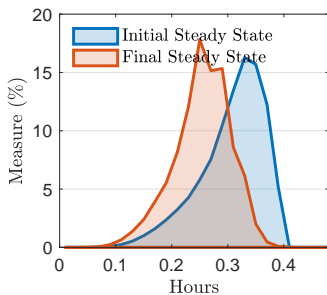
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Optimal plan Transitions and Welfare



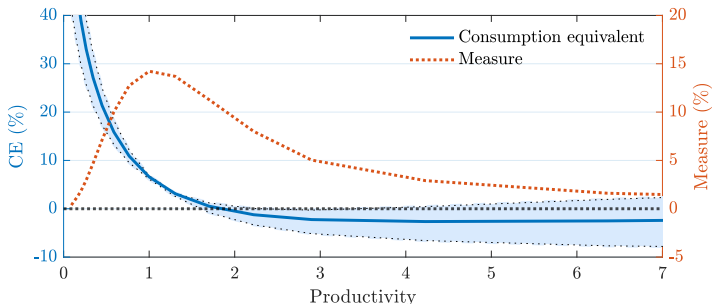
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o Welfare gains in CE terms: **+9.64%**!

- + Larger welfare gains for the poor
- + Decomposition: 70% insurance, 22% redistribution, 8% efficiency

How important is the phase-out of transfers?

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- Optimal plan with lump-sum transfers ($\xi = 0$)
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Lump-sum	Q1	Q2	Q3	Q4	Q5
Tax rate	56%	56%	57%	55%	58%
Transfer rate	181%	85%	53%	35%	13%

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⇒ Friedman was right!

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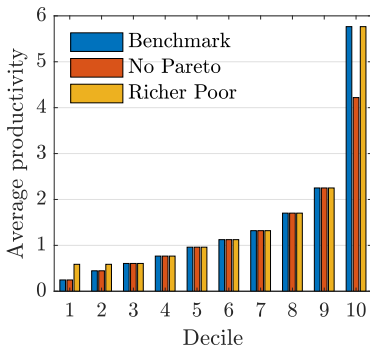
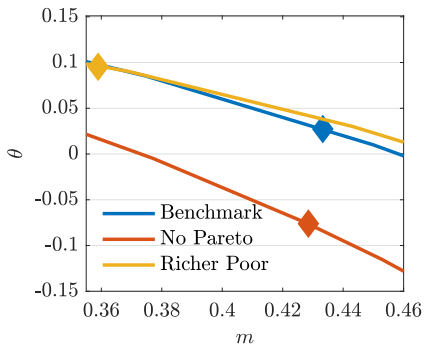
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- **Welfare gains** are **9.43%!** vs. 9.64% with phase-out
⇒ Friedman was right!... but marginal tax rates $> 60\%$!

Trading-off transfers vs. tax progressivity

Trading-off transfers vs. tax progressivity

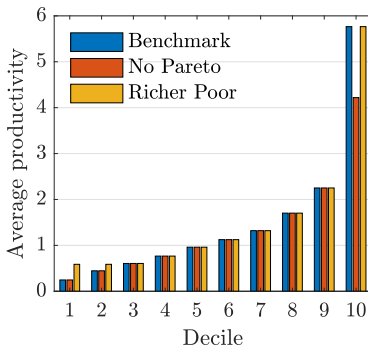
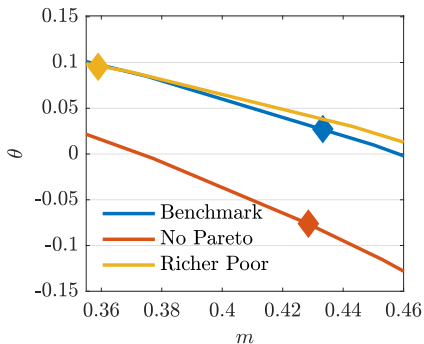
- Larger transfers are associated with lower progressivity



- The left tail pins down m , the right tail pins down θ

Trading-off transfers vs. tax progressivity

- Larger transfers are associated with lower progressivity



- The left tail pins down m , the right tail pins down θ
- Going further: risk (+) and wealth (+)

Conclusion

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Thank you!

Appendix

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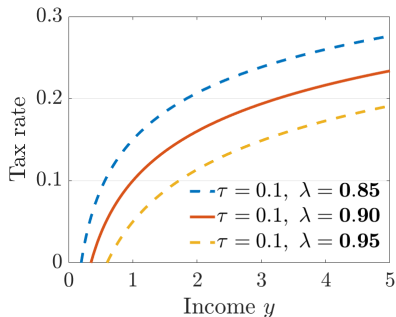
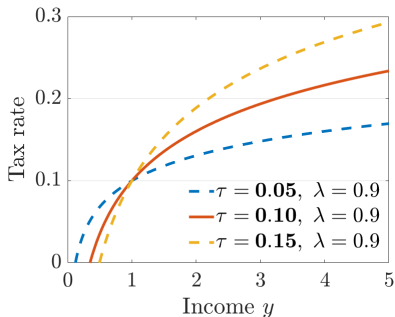
CBO Data: Components of Taxes and Transfers

- Broad measure of market income for non-elderly households
 - Labor and capital income
 - Includes all corporate and payroll taxes
- Taxes
 - Individual income tax (including tax credits) and payroll taxes
 - Corporate income tax and excise taxes
- Transfers
 - SNAP and other means-tested transfers (TANF, etc.)
 - Excluding SSI and Medicaid

Loglinear tax function Description

[< Back](#)

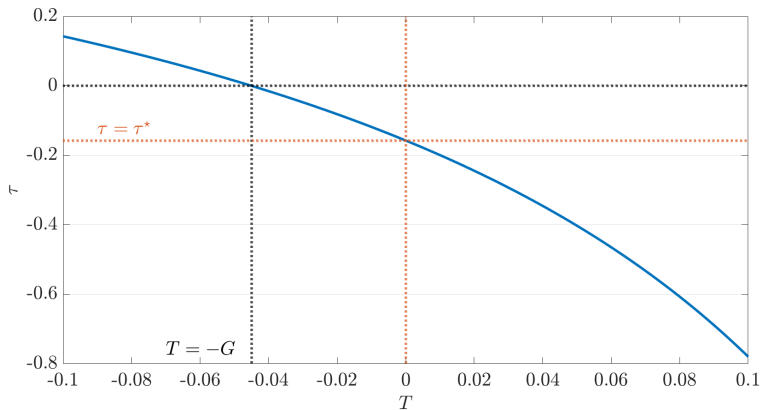
- A loglinear tax scheme: $\mathcal{T}(y) = y - \lambda y^{1-\tau}$
- Tax progressivity is captured by τ and level by λ



- Preference parameters: $\varphi^{-1} = 0.4$, B to match $n_0 = 0.3$
- Fiscal parameters: $\tau = 0.18$, $G/Y = 0.15$
- Idiosyncratic risk: $\rho_z = 0.935$, v_ω to match $\mathbb{V}[\log c]$

Transfers First-best

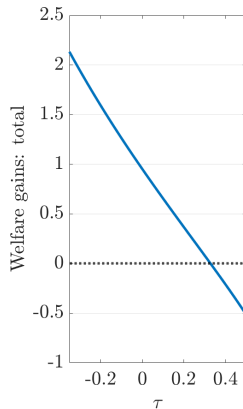
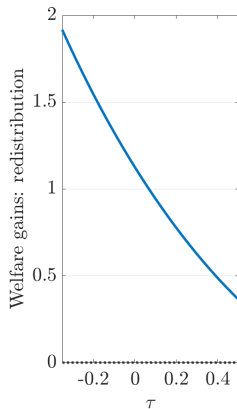
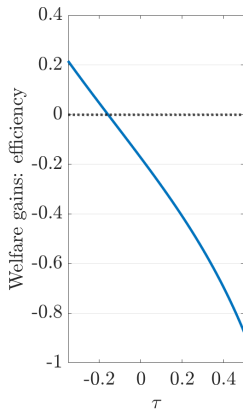
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Transfers

Heterogeneous agents

- **Negative** optimal relationship between T and τ



Equilibrium Definition

A stationary recursive competitive equilibrium is given by

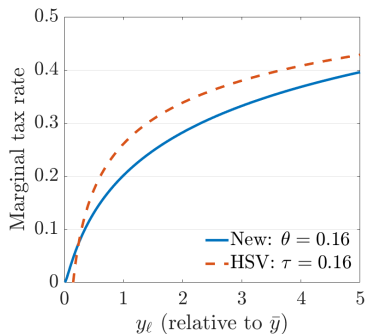
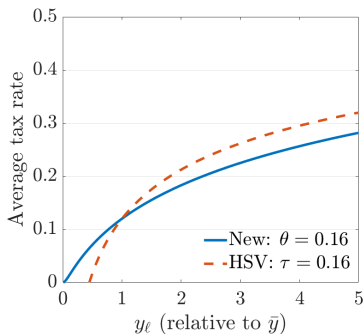
- Households' value functions $\{V\}$ and policies $\{c, a', n\}$. Firm's policies $\{L, K\}$.
- Government's policies $\{G, D, \lambda, \theta, m, \xi\}$
- A measure μ

such that given prices $\{r, w\}$

- Households and the firm solve their respective problems.
- The government's budget constraint holds.
- Markets clear
 - Capital market clears: $K + D = \int_{\mathcal{B}} a'(a, z) d\mu(a, z)$
 - Labor market clears: $L = \int_{\mathcal{B}} zn(a, z) d\mu(a, z)$
 - Goods market clears: $Y = \int_{\mathcal{B}} c(a, z) d\mu(a, z) + \delta K + G$
- Measure μ is stationary

$$\mu(a', z') = \int \mathbb{I}\{a'(a, z) = a'\} \pi_z(z'|z) d\mu(a, z)$$

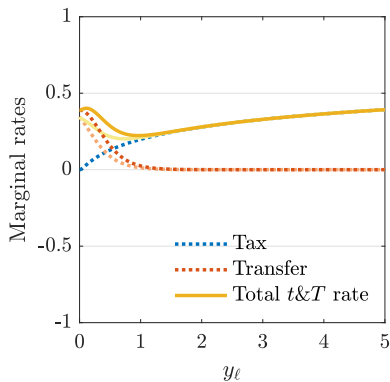
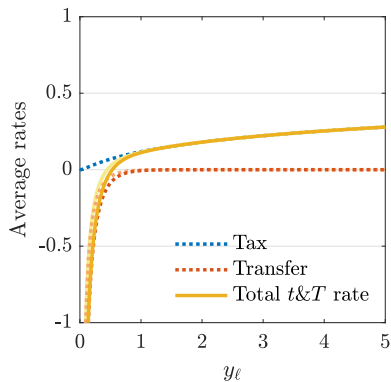
- New progressive labor tax resembles HSV except at the bottom



Calibration

- **Income process** to match **household** income risk
 - Annual earnings growth distribution from PSID (1978-1992)
 - + Std deviation: **0.35**, Skewness: **-0.45**, Kurtosis: **12**, P9010: **0.64**
 - $p_1 = 0.85$, $\mu_1 = 0.016$ ($\mu_2 = -0.091$), $\sigma_1 = 0.15$, $\sigma_2 = 0.63$
 - Persistence $\rho=0.935$ to match the **top-10** labor income **share**
- **Fiscal** parameters to match taxes and transfers per quintile
 - Taxes: $\theta = 0.16$, $\lambda = 0.12$
 - Transfers: $m = 0.19$, $\xi = 4.1$
- **Preferences**: $\sigma = 2$, $\varphi^{-1} = 0.4$; **Production**: $\alpha = 0.64$, $\delta = 0.08$
- Calibrate ($\beta = 0.962$, $B = 85$, $D = 0.59$) to match $r = 2\%$, $\bar{h} = 0.3$, $D/Y = 60\%$ ($\Rightarrow G/Y \approx 14\%$)

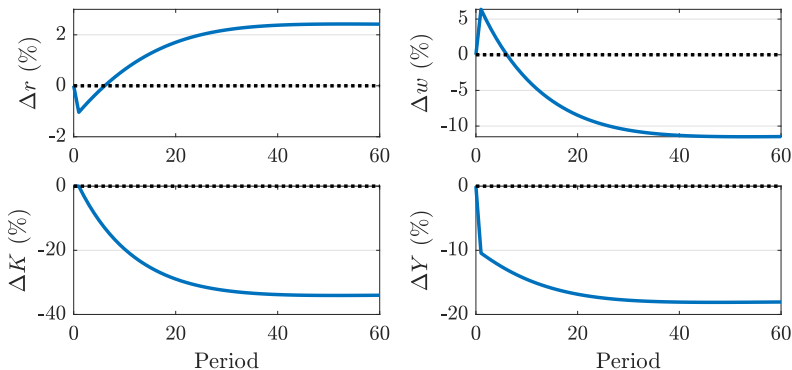
Calibration Fiscal system



■ Marginal rates by quintile: 33%, 24%, 21%, 23%, 31%

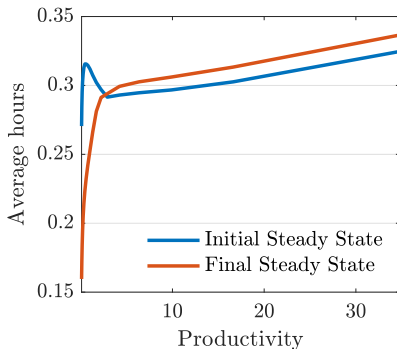
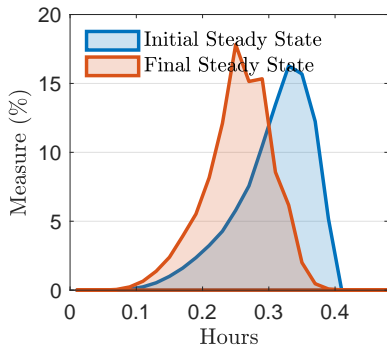
◀ Back

Transition to the optimal system



- Convergence achieved after ≈ 40 years

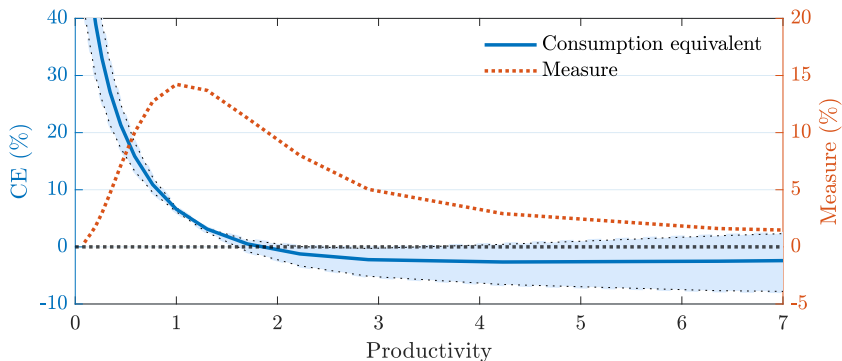
Transition to the optimal system



- The distribution of hours shift to the left

Optimal tax-and-transfer system ^{CE}

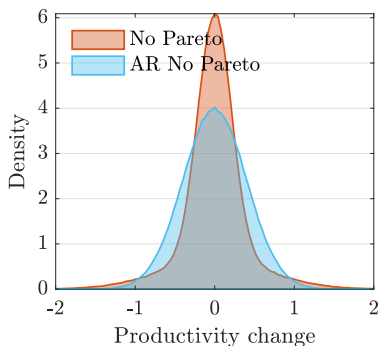
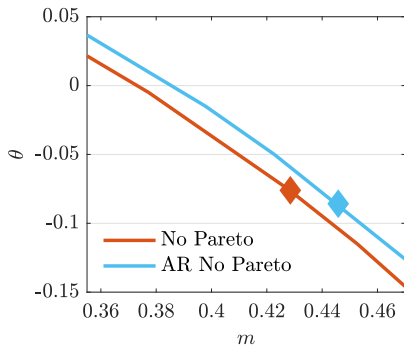
- Welfare gains: +9.62%, 79% households would benefit



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How important are departures from normality?

- The optimal system is **more generous** with AR(1) shocks!...

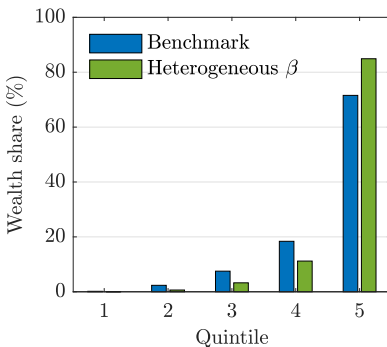
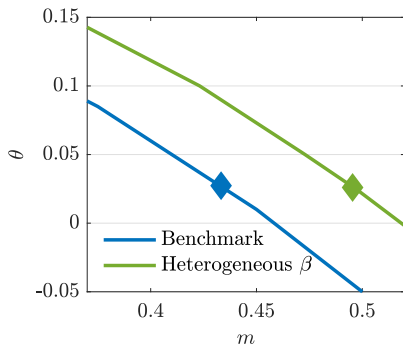


- Roughly similar progressivity.

Heterogeneous Beta

- Recalibration with heterogeneous stochastic discount factors

Krusell and Smith (1998)



- Larger transfers, robust m - θ relationship

◀ Back

Optimal loglinear plan

- Steady state: $\tau = 0.40$, with transitions: $\tau = 0.49$
- Consumption equivalent: $+5.08\%$

◀ Back

- Optimal plan without transition:

- $\theta = 0.03$, $m = 0.36$, $\xi = 0$

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